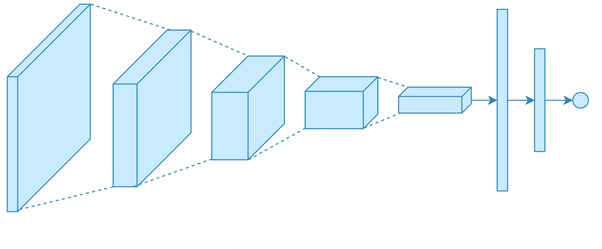


**Homework 2**

**Final Report**

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**Deep Learning**

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**Table of Contents**

**Introduction 3**

**Question 13**

1.1 3

1.2 4

1.3 5

1.3.1 5

1.3.2 6

**Question 27**

2.1 7

2.2 8

2.3 8

**Question 311**

3.1 a) 11

3.1 b) 11

3.1 c) 12

**Conclusion 12**

**Introduction**

The purpose of this project is to develop classification tasks, delving further into the topics of Convolutional Neural Networks (CNN) and the procedures of image captioning. These exercises allowed us to get in touch with new datasets and to apply the concepts and models learnt in class fully by ourselves.

**Question 1**

**Exercise 1.1**

**Input Image:** 28x28x3

**Convolutional Layer**:

* ­

­­­­

**Max Pooling Layer:**

**Linear Layer:**

* Flatten before the linear transformation,

Total

We can confirm this result using functions from Keras package

Graphical user interface, text, application, email

Description automatically generated

Table 1

**Exercise 1.2**

**1st Layer:**

* Flatten before the linear transformation,

**2nd Layer:**

Total

.

This shows one of the many advantages of using CNNs (with convolution and pooling layers) instead of fully connected layers. While in a fully connected all activations depend on all inputs, in a CNN this does not happen due to the filters used. For that reason, there are a many more parameters to be learned in the fully connected network, so a CNN is a much more viable solution, especially from the computational point of view.

**Exercise 1.3**

**Exercise 1.3.1**

Let’s consider the self-attention mechanism applied for a sequence of length L. In addition, let be the input matrix for this sequence, where n is the embedding size.

We can start by initializing a set of weights for the **keys**, a set of weights for the **queries** and a set of weights for the **values.**

We derive the **key, query** and **value** by considering the dot product between the input matrix by the respective weight matrix,

Now we can compute the attention scores and then convert these scores to probabilities via softmax transformation (row-wise),

In fact,

After showing that the self-attention probabilities for each head could be written in the required form, we conclude that:

We can find in the Literature[[1]](#footnote-1) that:

1. Rank of a matrix , ≤
2. If and then

By hypothesis,

* for with

So we conclude that,

**Exercise 1.3.2**

From the previous question, we found that

Starting with the first attention head,

For the second attention head,

But since

=

So the probabilities are the same, as we wanted to prove.

**Question 2**

**Exercise 2.1**

They convolutional layers[[2]](#footnote-2) – a key component of Convolutional Neural Networks (CNNs), can fancy a property called parameter sharing. This is a method of regularization where only a subset of parameters needs to be learned (and stored in memory). This particular property causes the layers to have another property called equivariance (to translation). In simple terms, to say a function is equivariant means that if the input changes, then the output changes in the same way. In mathematical terms:

is equivariant to a function if

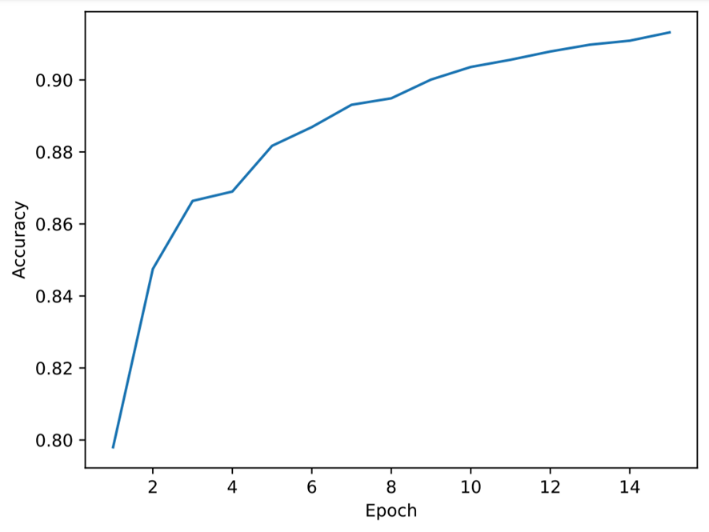
Considering a convolutional layer, if is a function that applies a translation to an object/input, the convolutional layer is equivariant to . This is not true if the operation is rotation or scale changes; this particular kind of operations require other mechanisms.

Exemplifying, if shifts each pixel of the image one pixel to right and then we apply convolution, the result will be the same as applying convolution first and then the shift operation.

In image processing this property is extremely useful. Since there is parameter sharing, an object will be detected independently of its position in the image, which is it’s something that will, most likely, happen in image classification problems of large datasets.

Chart

Description automatically generated**Exercise 2.2**

**** Figure 1 Figure 2

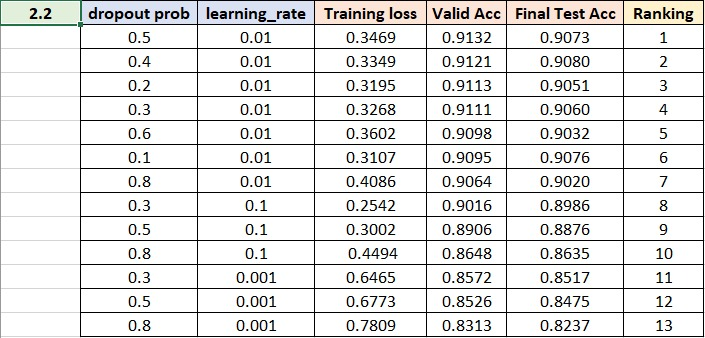
****

Table 2

**Exercise 2.3**

A picture containing calendar

Description automatically generated

Figure 3

Calendar

Description automatically generated

Figure 4

Each filter acts as a detector for a particular feature. The first layer filters mostly detect directions, colors, edges and simple shapes, so the results are not very detailed, as we can observe in Figure 5. These direction and color filters then get combined into basic grid and spot textures, so a little bit more detail becomes visible, like is shown in Figure 6.

As we go deeper into the network, the filters build on top of each other, and learn to encode more complex patterns. For example, in Figure 7, we can see a bird detector, where we observe multiple heads in different orientations, because the location of the bird in the image is not important, as long as it appears somewhere in the filter will activate.

That’s why the filter tries to detect the bird head in several positions by encoding it in multiple locations in the filter. This clearly illustrates that the model learns very detailed patterns near the output, i.e., in the final layers of the model, whereas more global and abstract ones are learnt in the early layers.

Chart, treemap chart

Description automatically generated

Figure 5

A picture containing calendar

Description automatically generated

Figure 6A group of birds

Description automatically generated with low confidence

Figure 7

**Question 3**

**Exercise 3.1 a)**

**Chart, line chart

Description automatically generatedChart, line chart

Description automatically generated**

Figure 9

Figure 8

The final test Bleu-4 value was 0.4981. The number can be observed in Figure 10.

A screenshot of a computer

Description automatically generated with medium confidence

Figure 10

**Exercise 3.1 b)Chart, line chart

Description automatically generatedChart, line chart

Description automatically generated**

Figure 11 Figure 12

The final test Bleu-4 value was 0.5142. The number can be observed in Figure 13.

**A screenshot of a computer

Description automatically generated with medium confidence**

Figure 13

**Exercise 3.1 c)**

The code used to plot the images and respective captions can be found in the Python Notebook “HW2\_c.ipynb”.



a residential area with houses arranged neatly and some roads go through this area

an industrial area with many white buildings and some roads go through this area

A curved river with some green waters and a highway passed by

**Conclusion**

Table 3

**Conclusion**

These classification problems represented great opportunities for us to have a more hands-on approach of the theoretical concepts and models presented in the classes, and allowed us to experiment and go further, understanding better the applications of Convolutional Neural Networks, which comprise a fundamental part of the theory behind unsupervised learning. Furthermore, these exercises generated a lot of discussion, because we were left in a situation where we could think by ourselves and come up with distinct suggestions and approaches.

Overall, these exercises were great learning experiences and provided knowledge that we will take for the rest of the trimester and eventually apply in our professional lives.

1. https://blogmedia.testbook.com/blog/wp-content/uploads/2016/09/Rank-of-a-Matrix-and-Its-Properties-GATE-Study-Material-in-PDF.pdf [↑](#footnote-ref-1)
2. Goodfellow, I., Bengio, Y. and Courville, A., 2017. Deep learning. Cambridge, Mass: The MIT Press. [↑](#footnote-ref-2)